Landscape complexity of the elastic manifold (or, when does a random interface behave like a glass?)

• Theorem (Ben Arous-Bourgade-M., after Fyodorov-Le Doussal):



• ... for the "elastic manifold," some model of random interfaces like



- which is interesting for the competition between elasticity (promoting flatness), mass (pro. location near 0), and disorder (pro. ruggedness),
- and where "glassy" (= complex) means there are many *metastable* states, or interface config.s locally minimizing EM Hamiltonian.